

SLIDE 15**Turning Repeating Decimals to Fractions**

Connect Your Learning!

You already know your decimal places (tenths, hundredths, thousandths, etc.) as well as the steps for turning a decimal into a fraction from our previous lesson.

Review Examples:

$$0.3 = \text{3 tenths or } \frac{3}{10}$$

$$2.48 = \text{2 and 48 hundredths}$$

$$2 \frac{48 \div 4}{100 \div 4} = 2 \frac{12}{25}$$

$$0.012 = \text{12 thousandths}$$

$$\frac{12 \div 4}{1000 \div 4} = \frac{3}{250}$$

For repeating decimals follow the same pattern. However, when you identify the decimal place (tenths, hundredths, etc) and make this your denominator subtract one.

For example: Instead of tenths you would use 9 and instead of 100 you would use 99.

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Make sure to take all notes/write down all steps when completing class examples so that you have information to refer to when you need help.

Write each decimal as a fraction in simplest form.

$$\frac{0.\overline{4}}{10 - 1} = \frac{4}{9}$$

$$\frac{0.\overline{45}}{100 - 1} = \frac{45}{99}$$

$$\frac{0.\overline{24}}{100 - 1} = \frac{24}{99}$$

$$\frac{0.\overline{53}}{100 - 10} = \frac{53 - 5}{90}$$

$$\frac{45 \div 9}{99 \div 9} = \frac{5}{11}$$

$$\frac{24 \div 3}{99 \div 3} = \frac{8}{33}$$

$$\frac{48 \div 6}{90 \div 6} = \frac{8}{15}$$

Converting Decimals to Fractions (A)

Name: _____

Date: _____

Convert each decimal to a fraction.

$$0.45 = \frac{45 \div 5}{100 \div 5} = \frac{9}{20}$$

$$0.\overline{18} = \frac{18}{100 - 1} \rightarrow \frac{18 \div 9}{99 \div 9} = \frac{2}{11}$$

$$0.3 = \frac{3}{10}$$

$$0.95 = \frac{95 \div 5}{100 \div 5} = \frac{19}{20}$$

$$0.8 = \frac{8 \div 2}{10 \div 2} = \frac{4}{5}$$

$$0.\overline{63} = \frac{63}{100 - 1} \rightarrow \frac{63 \div 9}{99 \div 9} = \frac{7}{11}$$

$$0.\overline{54} = \frac{54}{100 - 1} \rightarrow \frac{54 \div 9}{99 \div 9} = \frac{6}{11}$$

$$0.125 = \frac{125 \div 25}{1000 \div 25} = \frac{5 \div 5}{40 \div 5} = \frac{1}{8}$$

$$0.8\overline{3} = \frac{83 - 8}{100 - 10} \rightarrow \frac{75 \div 15}{90 \div 15} = \frac{5}{6}$$

$$0.9\overline{0} = \frac{90}{100 - 1} \rightarrow \frac{90 \div 9}{99 \div 9} = \frac{10}{11}$$

$$0.\overline{285714} = \frac{285,714}{1,000,000 - 1} = \frac{285,714}{999,999}$$

$$0.\overline{1} = \frac{1}{10 - 1} = \frac{1}{9}$$

$$0.\overline{3} = \frac{3}{10 - 1} \rightarrow \frac{3 \div 3}{9 \div 3} = \frac{1}{3}$$

$$0.1\overline{6} = \frac{16 - 1}{100 - 10} \rightarrow \frac{15 \div 15}{90 \div 15} = \frac{1}{6}$$

$$0.85714\overline{2} = \frac{857,142}{1,000,000 - 1} = \frac{857,142}{999,999}$$

$$0.\overline{4} = \frac{4}{10 - 1} = \frac{4}{9}$$

$$0.875 = \frac{875 \div 25}{1000 \div 25} = \frac{35 \div 5}{40 \div 5} = \frac{7}{8}$$

$$0.25 = \frac{25 \div 25}{100 \div 25} = \frac{1}{4}$$

$$0.42857\overline{1} = \frac{428,571}{1,000,000 - 1} = \frac{428,571}{999,999}$$

$$0.4 = \frac{4 \div 2}{10 \div 2} = \frac{2}{5}$$



Converting Repeating Decimals to Fractions

Name: _____

Rewrite each infinitely repeating decimal as a rational number (fraction).

1) $0.4\overline{354}$

$$\frac{4354 - 43}{10,000 - 100} = \frac{4311}{9,900}$$

2) $0.5\overline{88}$

$$\frac{588 - 58}{1000 - 100} = \frac{530}{900}$$

3) $0.6\overline{80}$

$$\frac{680 - 6}{1000 - 10} = \frac{674}{990}$$

4) $5.4\overline{84}$

$$\frac{484 - 48}{1,000 - 100} = \frac{436}{900} \div 4 = \frac{109}{225}$$

5) $8.1\overline{80}$

$$\frac{180 - 1}{1000 - 10} = \frac{179}{990}$$

6) $0.81\overline{668}$

$$\frac{81668 - 816}{100,000 - 1,000} = \frac{80,852}{99,000}$$

Answers

1. $\frac{4311}{9900}$

2. $\frac{53}{90}$

3. $\frac{674}{990}$

4. $5 \frac{109}{225}$

5. $8 \frac{179}{990}$

6. _____

7. _____

8. _____

9. _____

10. _____

7) $5.24\overline{690}$

$$\frac{24690 - 246}{100,000 - 100} \rightarrow \boxed{5 \frac{24,444}{99,000}}$$

8) $9.23\overline{31}$

$$\frac{2331 - 23}{10,000 - 100} \rightarrow \boxed{9 \frac{2308}{9,900}}$$

9) $27.9\overline{1}$

$$\frac{91 - 9}{100 - 10} \rightarrow \frac{82}{90} \div 2 = \boxed{27 \frac{41}{45}}$$

10) $4.59\overline{35}$

$$\frac{5935 - 593}{10,000 - 1,000} \rightarrow \boxed{\frac{5342}{90,000}}$$